

**Problem 1. – Lorentz Transformation**

Consider two inertial frame  $\Sigma, \Sigma'$  with parallel axes and relative speed  $\vec{v} = v \vec{e}_x$ . The transformation between  $\Sigma$  and  $\Sigma'$  is given by

$$\begin{pmatrix} x^{0'} \\ x^{1'} \end{pmatrix} = A(v) \begin{pmatrix} x^0 \\ x^1 \end{pmatrix}, \quad x^{2'} = x^2, \quad x^{3'} = x^3. \quad (1)$$

Find the matrix  $A(v)$  by using the 2. postulate of relativity, the linearity of the transformation, and  $A^{-1}(v) = A(-v)$ .

**Problem 2. – Relativistic Momentum- and Position operator**

The contravariant four-vectors of position and momentum are :  $x^\mu : \{ct, x, y, z\} = \{ct, \vec{r}\}$ ,  $p^\mu : \{\frac{E}{c}, p_x, p_y, p_z\} = \{\frac{E}{c}, \vec{p}\}$ . Find the form of the corresponding operators in position space and momentum space, that satisfy the commutation relation

$$[x^\mu, p^\nu] = -i\hbar g^{\mu\nu}$$

**Problem 3. – Klein-Gordon-Equation**

Show that the Klein-Gordon-Equation

$$-\hbar^2 \frac{\partial^2}{\partial t^2} \psi = (-\hbar^2 c^2 \Delta + m_0^2 c^4) \psi$$

remains invariant under Lorentz transformation.